

Unit 2 (2.1) Basics of Function Notes

- Domain: inputs or x-values
- Range: outputs or y-values
 - Domain (of a graph): From left to right
 - Range (of a graph): From bottom to top
 - Symbols:
 - From a table, ordered pairs, or mapping diagram use a list with {
 - For a graph ending in a ● use a [
 - For a graph ending in an arrow → or ○ use a (
 - Using an arrow also signifies no end to the graph, so use $-\infty$ or ∞
- Function: each x has exactly 1 y * all x-values must be different *
 - For graphs use the vertical line test

Function Notation

- $f(x), g(x), h(x) \dots$
 - is the same as y
 - means that the relation is a function
 - gives the equation a name
- $f(4)$ means to plug 4 in for x and simplify →

$$\begin{aligned} f(x) &= 2x - 6 \\ f(4) &= 2(4) - 6 \\ f(4) &= 8 - 6 \\ f(4) &= 2 \end{aligned}$$
- $g(h(-2))$ means to substitute twice. →

$$\begin{aligned} h(x) &= -3x + 8 \\ h(-2) &= -3(-2) + 8 \\ h(-2) &= 6 + 8 \\ h(-2) &= 14 \end{aligned} \rightarrow \begin{aligned} g(x) &= \frac{1}{2}x - 5 \\ g(14) &= \frac{1}{2}(14) - 5 \\ g(14) &= 7 - 5 \\ g(14) &= 2 \end{aligned}$$

*Start on the inside, work your way out

You try: If $k(x) = 2x^2 - 5$ and $m(x) = \frac{x}{4}$

Find a. $m(32)$

$$\begin{aligned} m(32) &= \frac{32}{4} \\ &= 8 \end{aligned}$$

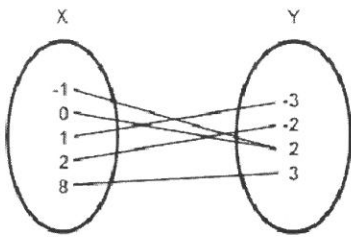
b. $k(-3)$

$$\begin{aligned} k(-3) &= 2(-3)^2 - 5 \\ &= 2(9) - 5 \\ &= 18 - 5 \\ &= 13 \end{aligned}$$

*c. $k(m(20))$

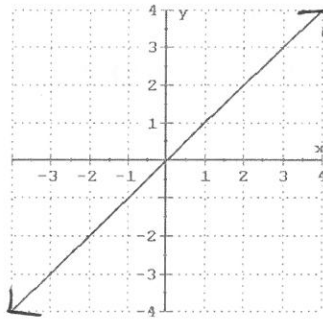
$$\begin{aligned} m(20) &= \frac{20}{4} = 5 \\ k(5) &= 2(5)^2 - 5 \\ &= 2(25) - 5 \\ &= 50 - 5 \\ &= 45 \end{aligned}$$

Functions



Domain: $\{-1, 0, 1, 2, 8\}$

Range: $\{-3, -2, 2, 3\}$



Domain: $(-\infty, \infty)$

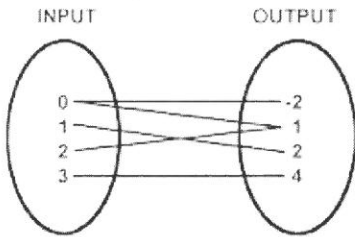
Range: $(-\infty, \infty)$

x	y
-2	-2
-1	2
0	6
1	10
2	14

Domain: $\{-2, -1, 0, 1, 2\}$

Range: $\{-2, 2, 6, 10, 14\}$

Not functions

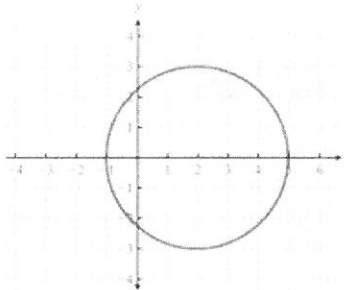


Domain:

$\{0, 1, 2, 3\}$

Range:

$\{-2, 1, 2, 4\}$



Domain:

$[-3, 3]$

Range:

$[-3, 3]$

X	Y
1	2
2	4
1	5
3	8
4	4
5	10

Domain:

$\{1, 2, 3, 4, 5\}$

Range:

$\{2, 4, 5, 8, 10\}$

Determine whether each relation is a function and then state the domain and range.

Function?
 Y or N

Domain: $\{5, 10, 15\}$

Range: $\{105, 110\}$

Function?
 Y or N

x	y
-2	-1
-2	1
-1	0
1	0
2	1

Domain: $\{-2, -1, 1, 2\}$

Range: $\{-1, 1, 0\}$

Function?
 Y or N

Domain: $\{-3, -2, -1, 3\}$

Range: $\{4, -1\}$

$\{(-3, 4), (-2, 4), (-1, -1), (3, -1)\}$

Function?
 Y or N

Domain: $[0, \infty)$

Range: $[0, \infty)$

Function?
 Y or N

Domain: $(-\infty, \infty)$

Range: $[0, \infty)$

Function?
 Y or N

Domain: $[0, \infty)$

Range: $(-\infty, \infty)$

Function?

Y or (N)

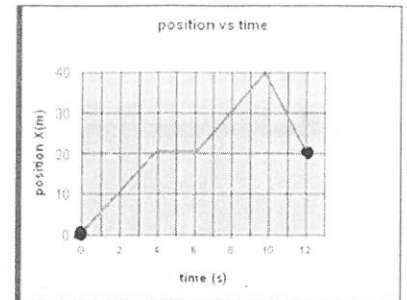
x	y
-4	-4
-2	-2
1	0
1	1

Domain: $\{-4, -2, 1\}$

Range: $\{-4, -2, 0, 1\}$

Function?

(Y) or N



Domain: $[0, 12]$

Range: $[0, 40]$

$(-5,6) (-10,7) (3,8) (5,6) (-5,7)$

Function?

Y or (N)

Domain: $\{-5, -10, 3, 5\}$

Range: $\{6, 7, 8\}$

Function?

(Y) or N

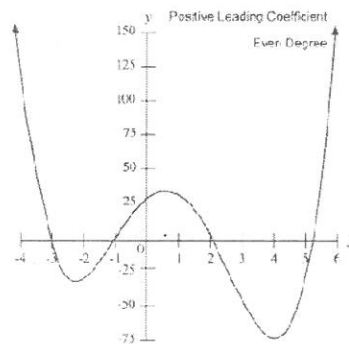
x	y
1	2
2	4
3	6

Domain: $\{1, 2, 3\}$

Range: $\{2, 4, 6\}$

Function?

(Y) or N



Domain: $(-\infty, \infty)$

Range: $[-75, \infty)$

Function?

(Y) or N

$$y = x^3 + 2x^2 - 1$$



Domain: $(-\infty, \infty)$

Range: $(-\infty, \infty)$